## 國 立 清 華 大 學 命 題 紙

八十八學年度 **化學系** 系 (所) 化學、為化 組碩士班研究生招生考試 科目 物理化:學及分析化學 科號 8683 共 5 頁第 1 頁 \*請在試卷【答案卷】內作答

- (5%) 1. Describe the preparation of 100 mL of the diluted HNO<sub>3</sub> acid solution with a mole ratio of one HNO<sub>3</sub> to three H<sub>2</sub>O from a concentrated solution that has a specific gravity of 1.42 and is 70% HNO<sub>3</sub> (w/w). The specific gravity of the pure nitric acid is 1.50.
- (5%) 2. Calculate the standard deviation of the result of  $\frac{[14.3(\pm0.2)-11.6(\pm0.2)]\times0.050(\pm0.001)}{[8.20(\pm10)+1030(\pm5)]\times42.3(\pm0.4)}=1.725(\pm?)\times10^{-6}$
- (5%) 3. A new procedure for the rapid determination of sulfur in kerosenes was tested on a sample known from its method of preparation to contain 0.123% S. The results were % S = 0.112, 0.118, 0.115, and 0.119. Do the data indicate that there is a bias in the method?
- (5%) 4. Find the conditions under which Cd<sup>2+</sup> and Tl<sup>+</sup> can, in theory, be separated quantitatively with H<sub>2</sub>S from a solution that is 0.1 M in each cation. The saturated concentration of H<sub>2</sub>S is 0.10 M. The equilibrium constants of the relevant reactions are:

$$\begin{split} H_2S + H_2S &= - H_3 \overset{+}{O} + HS^- & K_1 = \frac{[H_3 \overset{+}{O}][HS^-]}{H_2S} = 9.6 \times 10^{-8} \\ HS^- + H_2O &= - H_3 \overset{+}{O} + S^2 - K_2 = \frac{[H_3 \overset{+}{O}][S^2^-]}{[H_2S^-]} = 1.3 \times 10^{-14} \\ CdS_{(8)} &= - Cd^{2+} + S^{2-} & K_{sp} = [Cd^{2+}][S^{2-}] = 1 \times 10^{-27} \\ Tl_2S_{(8)} &= - 2Tl^+ + S^{2-} & K_{sp} = [Tl^+]^2[S^2^-] = 6 \times 10^{-22} \end{split}$$

八十八學年度 **化學系** 系(所) 化學、為化組碩士班研究生招生考試 科目 物理化學及分析化學 科號 0503 共 5 頁第 2 頁 \*請在試卷【答案卷】內作答

(5%) 5. Derive a titration curve for the reaction of 50.00 mL of 0.02500 M U<sup>4+</sup> with 0.1000 M Ce<sup>4+</sup> by adding 5.00 mL. 12.5 mL and 25.10 mL of Ce<sup>4+</sup>. The solution is 1.0 M in H<sub>2</sub>SO<sub>4</sub> throughout the titration (for the sake of simplicify, assume that [H+] for this solution is also about 1.0 M)

$$Ce^{4+} + e^{-} \implies Ce^{3+} \qquad E^{0} = +1.44 \text{ V}$$

$$UO_{2}^{2+} + 4H^{+} + 2e^{-} \implies U^{4+} + 2H_{2}O \qquad E^{0} = +0.334 \text{ V}$$

- (5%) 6. A Cell consisting of a saturated calomel electrode and a lead ion electrode developed a potential of -0.4706 V when immersed in 50.00 mL of a sample. A 5.00 mL addition of standard 0.0200 M lead solution caused the potential to shift to -0.4490V. Calculate the molar concentration of lead in the sample.
- (5%) 7. Describe the following components of the optical instrument:
  - (a) monochromator
  - (b) filter
  - (c) phototube
  - (d) photomultiplier
  - (e) photovoltaic cell
- (5%) 8. Identify factors that cause the Beer's law relationship to depart from linearity.
- (5%) 9. Substances A and B have retention times of 16.40 and 17.63 min, respectively, on a 30.0 cm column. An unretained species passes through the column in 1.30 min. The peak widths (at base) for A and B are 1.11 and 1.21 min, respectively. Calculate (a) column resolution, (b) average number of plates in the column, (c) plate height, (d) length of column required to achieve a resolution of 1.5, and (e) time required to elute substance B on the longer column.

八十八學年度 化學系 系 (所) 在學·為在組織土班研究生招生考試 科目 物理化學及分析化學 科號 8583 共 5 頁第 3 頁 \*請在試卷【答案卷】內作名

(5%) 10. A GC experiment has been run to determine the optimal gas flow as shown in the following table:

Chromatogram	Gas flow (mlmin <sup>-1</sup> )	Retention time (min)	Base width (min)
A	4.0	21.0	4.0
: B	3.5	23.0	4.0
C	3.0	26.5	4.0
D	2.5	32.0	4.0
E	2.0	40.0	6.0
F	1.5	44.0	8.0

- (a) Plot the HETP vs. Gas flow (V) and find the optimal gas flow. (assume the column length is 10 m)
- (b) Use the Van Deemter equation to explain the relationship between HETP and V and elaborate the each term in the Van Deemter equation.
- (4%) 11. Suppose that an oscillator (with the reduced mass μ) is governed by the potential

$$V(\mathbf{x}) = \begin{cases} \frac{\mathbf{k}}{2} \mathbf{x}^2 & 0 \le \mathbf{x} \le \mathbf{a} \\ \infty & \text{otherwise} \end{cases}$$

- (a) What are the eigenfunctions? You only have to solve it in terms of the wavefunctions of one dimensional harmonic oscillator with the proper constraints and modifications if it is necessary.
- (b) What are the corresponding eigenvalues?

八十八學年度 化學系 系 (所) 化學·萬化 組碩士班研究生招生考試 科目 物理化學及分析化學 科號 8583 共 5 頁第 4 頁 \*請在試卷【答案卷】內作答

(10%) 12. Briefly explain the terms or answer the following questions.

- (a) selection rule of electronic spectra
- (b) when do two operators commute?
- (c) uncertainty principle
- (d) Hund's rule
- (e) singlet state
- (12%) 13. Two mole of an ideal monatomic gas at 27°C and 3.0 L is allowed to expand isothermally, i.e. the temperature T is fixed, for the following two processes, (1) into an evaculated bulb, and (2) reversibly, to a total volumn of 5.0 L. What are q, w, ΔE, ΔH, ΔG, and ΔS for each process?
- (4%) 14. Using the relationship

$$\ln(K) = -\frac{\Delta H^{o}}{RT} + \frac{\Delta S^{o}}{R}$$

discuss how would a system at equilibrium shift when the temperature is changed.

(10%) 15. An electrochemical cell has 0.1 M  $Zn^{2+}$  in the anodic compartment, and  $[VO_{2^+}] = 2.0$  M,  $[VO^{2+}] = 0.01$  M,  $[H^+] = 0.5$  M in the cathodic compartment (see the figure shown below. Given that  $T = 25^{\circ}C$ 

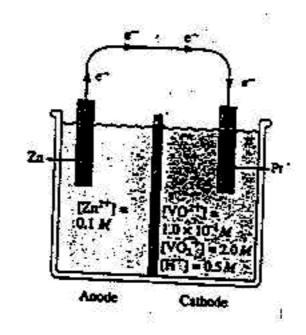
$$VO_2^+ + 2H^+ + e^- \longrightarrow VO^{2+} + H_2O \qquad E^0 = 1.00 \text{ V}$$
 (1)

$$Z_0^{2+} + 2e^- \longrightarrow Z_0$$
  $E^0 = -0.76 \text{ V}$  (2)

Calculate the voltage which the electrochemical cell can provide.

## 國立清華大學命題紙

八十八學年度 化學系 系 (所) 化學、無此組織上班研究生招生考試 科目 物理化學及分析化學 科號 8503 共 5 頁第 5 頁 \* 簡在試卷【答案卷】內作名



(10%) 16. Based on the Michaelis-Menton model for noncompetitive inhibition shown below:

$$E + S = \frac{k_1}{k_2} [ES] \xrightarrow{k_3} E + P$$

$$+[I]^{k_4} k_6$$
[EI]

Show that  $1/V = 1/V_{max} + (K_M/V_{max}) \cdot (1+[I]/K_i) \cdot (1/[S])$ , where V = dP/dt, Michaelis constant  $K_M = (k_2 + k_3)/k_1$ , and inhibition constant  $K_i = k_5/k_4$ .