台灣聯合大學系統102學年度碩士班招生考試命題紙 共了 頁第一頁

科目: 物理化學(1004)

校系所組:中央大學化學學系

交通大學應用化學系 (甲組)

清華大學化學系

清華大學材料科學工程學系(丙組)

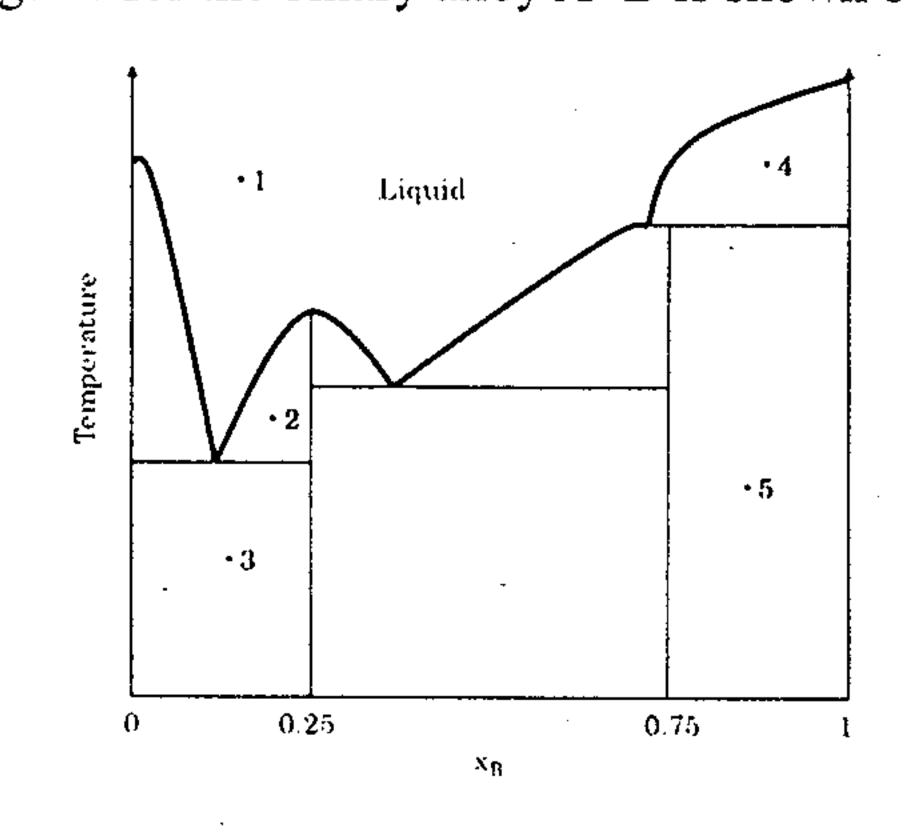
- 1. (15%) Calculate the work, heat, energy, enthalpy, entropy, and Gibbs free energy of one mole ideal gas that undergoes reversible isothermal compression from V to V/2.
- 2. (10%) Starting with the virial equation for a real gas in the following form

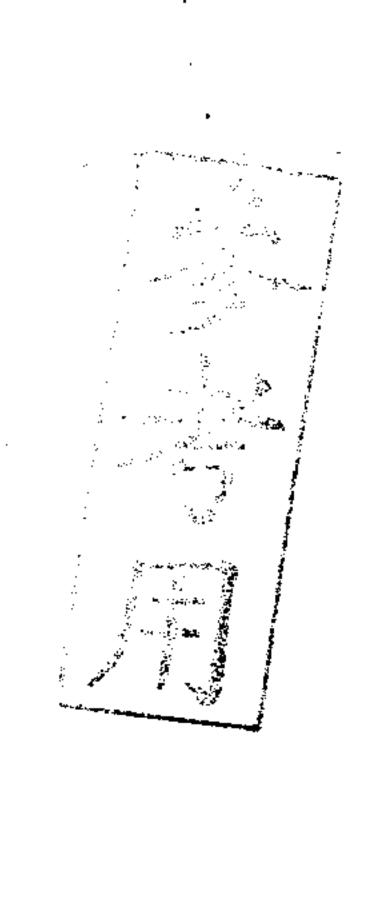
$$PV_m = RT \times (1 + \frac{B(T)}{V_m})$$

V_m and B(T) represent the molar volume and temperature-dependent virial coefficient, respectively. If the sample undergoes isothermal expansion from V to 2V,

(1) Derive "X" and "Y" for
$$\left(\frac{\partial H}{\partial V}\right)_T = X\left(\frac{\partial P}{\partial V}\right)_T + Y\left(\frac{\partial P}{\partial T}\right)_V$$
. (4 %)

- (2) Derive $\left(\frac{\partial H}{\partial V}\right)_T$ in terms of B, T, V, R, and $\frac{\partial B}{\partial T}$. (3 %)
- (3) Derive the molar enthalpy change (ΔH_m). (3 %)
- 3. (9%) A phase diagram for the binary alloy A+B is shown below.





XB represents the molar fraction of component B. Please answer the questions (a)-(c).

Point	Composition
1	Liquid
2	(a)
3	(b)
4	(c)
5	Pure $B_{(s)} + AB_{3(s)}$

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4. (8%) A hypothetical chain reaction leads to a complicated rate law.

$$A_2 + B_2 \rightarrow 2 \text{ AB}$$

$$\frac{d[AB]}{dt} = \frac{k_1[A_2][B_2]^{3/2}}{[B_2] + k_2[AB]}$$

The reaction mechanism is defined as a proposed set of elementary steps:

Initiation:
$$B_2 + M \stackrel{k_a}{\to} B + B + M = \frac{1}{2} \frac{d[B]}{dt} = k_a[M][B_2]$$

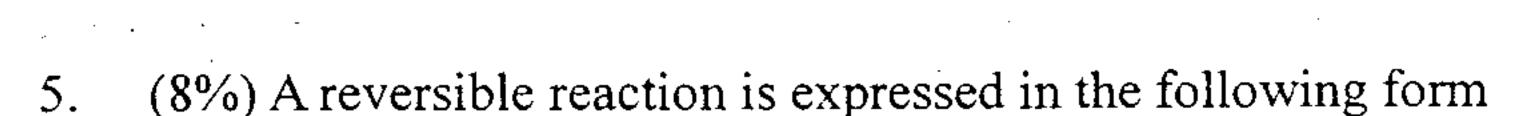
Propagation: B + A₂
$$\stackrel{k_b}{\rightarrow}$$
 AB + A $\frac{d[AB]}{dt} = k_b[A_2][B]$

$$A + B_2 \stackrel{k_c}{\rightarrow} AB + B \quad \frac{d[AB]}{dt} = k_c[A][B_2]$$

Inhibition: A + AB
$$\stackrel{k_d}{\rightarrow} A_2 + B$$
 $\frac{d[AB]}{dt} = -k_d[A][AB]$

Termination: B + B + M
$$\stackrel{k_e}{\rightarrow} B_2 + M$$
 $\frac{1}{2} \frac{d[B]}{dt} = -k_e[B]^2[M]$

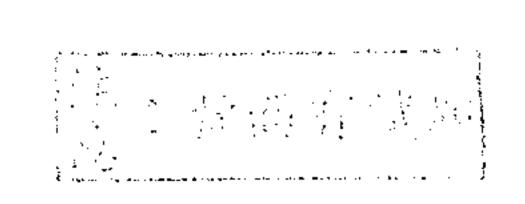
Derive k_1 and k_2 in terms of k_a , k_b , k_c , k_d , and k_e when applying the steady-state approximation on d[A]/dt and d[B]/dt.



$$A \xrightarrow{k_f} B$$

The initial concentrations of A and B are $[A]_0$ and 0, respectively. k_f and k_r represent the first-order rate coefficients of the forward and backward reactions, respectively.

- (1) Derive the time dependence of [A] and [B]. (4 %)
- (2) Derive the concentrations of [A] and [B] at equilibrium. (4%)
- 6. (10%) Explain the method of using half-life times to derive the order of a chemical reaction for the 0-, 1st-, and 2nd-order reaction. Please write down the proper equation to describe your method.
- 7. (5%) For the gas-phase reaction H₂ + Br₂ → 2HBr at 373.15 K, the rate constant is equal to 8.75× 10⁻¹⁵ L mol⁻¹s⁻¹. At 473.15 K it is equal to 9.53× 10⁻¹⁵ L mol⁻¹s⁻¹. Show all the details for how to find the value of the activation energy and of the preexponential factor.



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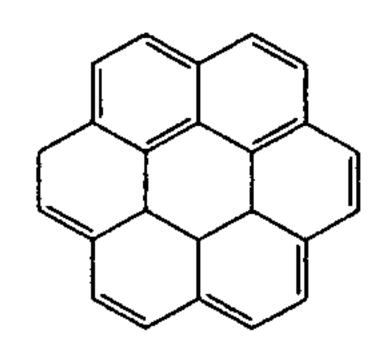
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8. (7%) For (1) B₂, and (2)H₂O₂ molecules, determine (a) the point group, (b) the term symbol of ground state, (c) whether it has a permanent dipole moment, (d) whether it is optically active, (e) whether it is microwave spectrum active.

- 9. (20%) The partition function is the fundamental concept of statistical thermodynamics.
 - (1) For an ideal gas, define the molar partition function, Q, by partition function of one partical, q.
 - (2) The Hamiltonian of an individual molecule can be simplified based on Born-Oppenheimer approximation. What is the Born-Oppenheimer approximation?
 - (3) Describe the result of the simplified Hamiltonian based on Born-Oppenheimer approximation.
 - (4) For each part of (3) state a proper model to botain the eigenvalues, *i.e.*, energy levles.
 - (5) What is the partition function of a molecule, q? Express it with degneracy and energy level. (You do not have to do the summation or integration.)
- 10. (8%) The molecule cocronen



is quite often used as a very simple modle of graphene. Show how you will calcualte the frequency of the π electron transition. The carbon-carbon distance is 1.33Å.

