

國 立 清 華 大 學 命 題 紙

95 學年度 生醫工程與環境科學系 系(所) 丙 組碩士班入學考試

科目 近代物理 科目代碼 3202 共 2 頁第 2 頁 *請在【答案卷卡】內作答

8. (6) What are the two main differences between the classical and quantum theory of conduction in metals?

9. (6) To what voltage must we accelerate electrons (for example, in electron microscope) if we wish to resolve a protein of diameter 4nm?

10. (10) The decay between two excited states of the nucleus of ^{48}Ti emits gamma ray of 1.3117 MeV. The upper state has a lifetime of 1.4ps, the lower state 3.0 ps. A) What is the fractional uncertainty $\Delta E/E$ in the energy of the gamma ray? B) What is the percentage spread in wavelength of the gamma ray ($\Delta\lambda/\lambda$)?

11. (10) The ground state wave function of Hydrogen atom is $\psi_{100}=C_{100}e^{-r/a_0}$. What is the radial probability distribution function $P(r)$ for this state? Show that $P(r)$ has its maximum value at $r=a_0$.

12.(10) Determine the mass of a free particle whose wave function is the plane wave

$$\psi(x, t) = Ae^{i(2.5 \times 10^{11} x - 2.1 \times 10^{13} t)}$$

where distance is in meters and time in seconds.

13. (15) Assume that a neutron decays into a proton plus an electron without a neutrino. A) Assume that the kinetic energy of the electron is 0.8 MeV and calculate the momentum p of the electron in MeV/c. B) From momentum conservation, calculate the kinetic energy of the proton. C) In this situation, the energy shared by the proton and electron is 0.8 MeV. Calculation in B) gives a correction to the assumption of the energy of the electron to be 0.8 MeV. What percentage of 0.8 MeV is this correction?