台灣聯合大學系統105學年度碩士班招生考試試題

類組: <u>電機類</u> 科目: <u>電磁學 B(3008)</u>

共_2 第 第 / 頁

※請在答案卷內作答

1. (10%) A laser beam in some liquid has its electric field described as the following:

$$\vec{E}(t,z) = \hat{a}_x 3\cos(6\pi \times 10^{14}t - 4\pi \times 10^6z) - \hat{a}_y 3\sin(6\pi \times 10^{14}t - 4\pi \times 10^6z) \quad (V/m)$$

Answer the following questions:

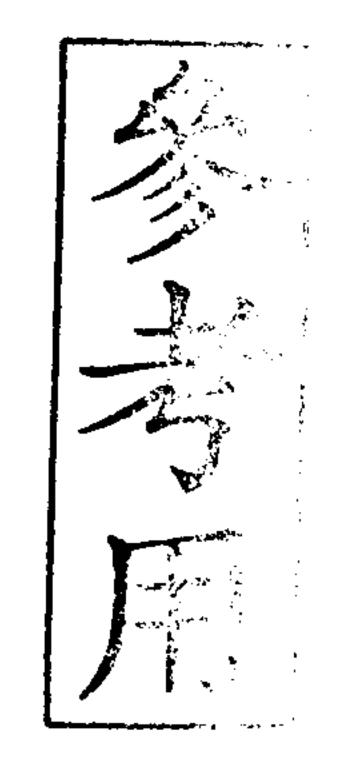
- a. What is the polarization status? (2%)
- b. What is the propagation direction? (2%)
- c. What is its wavelength and frequency in the liquid? (2%)
- d. What is the phase velocity in this liquid? (2%)
- e. Is this laser beam a UV, visible, near-infrared, mid-infrared, or far-infrared light (2%)?
- 2. (10%) Given that $\vec{H} = \hat{a}_y 2 \sin(6\pi \times 10^9 t \beta z)$ (A/m) in air (source free), find (a)

$$\bar{E}$$
 (5%) and (b) the power density (5%). ($\varepsilon_o \sim \frac{1}{36\pi} \times 10^{-9}$ F/m)

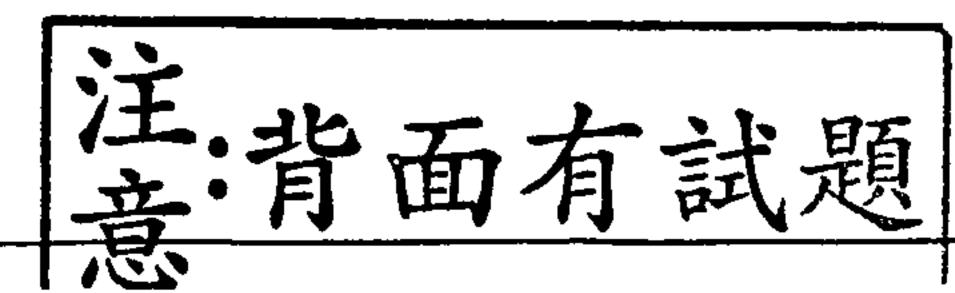
- 3. (10%) What is the fundamental mode of a planar metallic waveguide?
- 4. (10%) Calculate the capacitance of two concentric spherical shells of radii a and radii b. The inner shell is at the potential of V_o , the outer shell is grounded, and the dielectric constant of the material between the two shells is ε .
- 5. (10%) The normalized radiation intensity of a certain antenna is given by

$$F(\theta) = \begin{cases} \cos^2 \theta, \text{ for } 0 \le \theta \le \frac{\pi}{2} \\ 0, \text{ for } \frac{\pi}{2} \le \theta \le \pi \end{cases}$$

, where $\, heta\,$ is in radian. Determine the half-power beamwidth $\,eta\,$.



- 6. (10%) When sunlight reflected from the surface of water is viewed through a linearly polarizing glass, the apparent glare from the water is reduced.
 - (a) Suppose you have a beachfront house, and you want to use polarizing glass to reduce the glare from the sunlight reflected from the ocean. How should you



類組: <u>電機類</u> 科目: <u>電磁學 B(3008)</u>

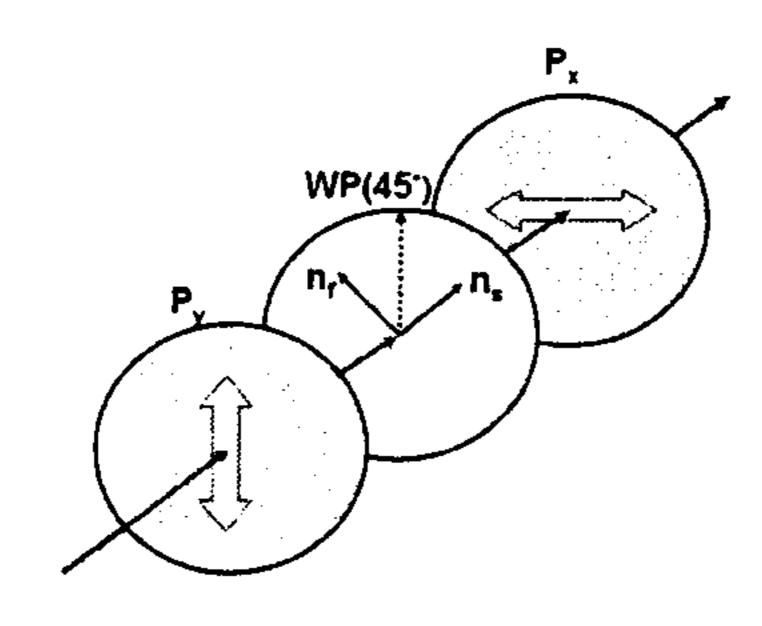
共 2 頁 第 2 頁

※請在答案卷內作答

orient the polarizing glass to obtain the optimized reduction of the glare? (5%) (Please describe it in terms of the orientation of the transmission axis)

- (b) From which angle of reflected sunlight will you polarizing glass be most effective? (5%) (Assume that the index of refraction of water is 1.33.)
- 7. (10%) Consider an input plane wave with optical intensity I₀, and left-handed circularly polarized, passing through the following set of 3 optical elements (i.e., a half wave-plate rotated by 45° sandwiched between a pair of cross-polarizers).

 Calculate the optical intensity of the output wave.



8. (10%) A plan wave traveling in a medium 1 with $\varepsilon_{r1} = 4.00$ is incident to a medium 2 with $\varepsilon_{r2} = 2.25$. Both media are non-magnetic and non-conductive. Now the electric field of the normal incident EM field is described as

$$\vec{E}_i = \hat{y}8\cos(4\pi \times 10^{14}t - \beta z) \quad (V/m).$$

- (a) What is the electric field of the reflected wave? (5%)
- (b) What is the value of β ? (5%)
- 9. (10%) A 50Ω lossless transmission line is to be matched to a resistive load impedance with $Z_L = 300\Omega$ via a quarter-wave section, thereby eliminating the reflections along the feedline. Find the required characteristic impedance of the quarter-wave transformer.
- 10. (10%) Given that the skin depth for graphite(石墨) at 100 MHz is 0.16 mm, determine the distance that a 100 MHz wave travels in graphite such that its field intensity (power) is reduced by 30 dB.

