注意:考試開始鈴響前,不得翻閱試題,

並不得書寫、畫記、作答。

國立清華大學108學年度碩士班考試入學試題

系所班組別:資訊**工**程學系

考試科目(代碼):基礎計算機科學(2301)

一作答注意事項-

- 1. 請核對答案卷(卡)上之准考證號、科目名稱是否正確。
- 作答中如有發現試題印刷不清,得舉手請監試人員處理,但不得要求解 釋題意。
- 考生限在答案卷上標記「由此開始作答」區內作答,且不可書寫姓名、 准考證號或與作答無關之其他文字或符號。
- 4. 答案卷用盡不得要求加頁。
- 5. 答案卷可用任何書寫工具作答,惟為方便閱卷辨識,請儘量使用藍色或 黑色書寫;答案卡限用 2B 鉛筆畫記;如畫記不清(含未依範例畫記) 致光學閱讀機無法辨識答案者,其後果一律由考生自行負責。
- 其他應考規則、違規處理及扣分方式,請自行詳閱准考證明上「國立清 華大學試場規則及違規處理辦法」,無法因本試題封面作答注意事項中 未列明而稱未知悉。

系所班組別:基礎計算機科學

考試科目 (代碼):2301

共_4_頁,第_1_頁 *請在【答案卷、卡】作答

- 1. (10%) Use generating functions to answer the following questions.
 - (A) (7%) Find the solution of the recurrence relation $a_n=4a_{n-1}-3a_{n-2}+2^n+n+3$ with $a_0=1$ and $a_1=4$.
 - (B) (3%) Find the coefficient of x^{10} in the power series of $x^4/(1-3x)^3$.
- 2. (10%) How many relations are there on a set with *n* elements that are
 - (A) (5%) both reflexive and symmetric?
 - (B) (5%) neither reflexive nor irreflexive?
- 3. (5%) How many nonisomorphic unrooted trees are there with five vertices?
- 4. (5%) Multiple answer question. (It is possible that more than one of the choices are correct. Find out all correct choices.)

A hash table of length 10 uses the hash function $h(k) = k \mod 10$ and the **linear probing** for handling overflow. After inserting 6 values into an initiallyempty hash table, the table is as shown below. Which one(s) of the following choices gives a possible order in which the key values could have been inserted in the table?

0	
1	
2	42
3	23
4	34
5	52
6	46
7	33
8	
9	

- (A) 46, 42, 34, 52, 23, 33
- (B) 34, 42, 23, 52, 33, 46
- (C) 46, 34, 42, 23, 52, 33
- (D) 42, 46, 33, 23, 34, 52
- (E) 42, 23, 34, 46, 52, 33

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考試科目 (代碼):2301

共_4_頁,第_2_頁 *請在【答案卷、卡】作答

5. (5%) <u>Fill in</u> the six blanks (I, II, ..., and VI) in the following program that implements a *queue* by using 2 *stacks*.

```
class MyQueue<T>{
private:
    stack<T> stack1;
    stack<T> stack2;
public:
    MyQueue()
    {
         stack1 = new stack<T>();
         stack2 = new stack<T>();
    // enqueue(): Add an element at the rear side of MyQueue
    void enqueue(T e)
    {
         stack1.push(e);
    }
    // dequeue(): Remove the front element from MyQueue
    T dequeue(T e)
    {
         if( (___) .isEmpty() )
              while( !(_____).isEmpty() )
                  (<u>III</u>).push((<u>IV</u>).pop());
         T temp = null;
         temp = (______).pop();
         return temp;
    }
```

6. (5%) AVL Tree.

(A) (2%) Please draw how an initially-empty AVL tree would look like after sequentially inserting the integer keys 100, 200, 50, 300, 400. There is no need to show it in a step-by-step fashion; you only need to draw the final result.

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共<u>4</u>頁,第<u>3</u>頁 *請在【答案卷、卡】作答

- (B) (3%) Continue the previous sub-problem. Suppose that the integer keys 25, 250, 225, 500, 240, 260 are sequentially inserted into the AVL tree of the previous sub-problem. Draw the AVL tree after all of these integer keys are inserted.
- (5%) Reconstruct and draw the maximum binary heap whose in-order traversal is
 2, 16, 7, 62, 5, 9, 188, 14, 78, 10. There is no need to show it in a step-by-step fashion; you only need to draw the final result.
- 8. (5%) The following algorithm takes an array as input and returns the array with all the duplicate elements removed. For example, if the input array is {1, 3, 3, 2, 4, 2}, the algorithm returns {1, 3, 2, 4}.

S = new empty set
A = new empty dynamic array
for every element x in input array
if not S.member(x) then
S.insert(x)
A.append(x)
return A

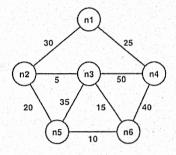
Suppose that the input array has *n* elements. What is the big-O complexity of this algorithm, if the set S is implemented as:

- (A) (1%) a hash table (with the assumption that overflow does not occur)?
- (B) (2%) a binary search tree?
- (C) (2%) an AVL tree?
- 9. (10%) The recurrence $T(n) = 7T\left(\frac{n}{2}\right) + n^2$ describes the running time of an algorithm A. A competing algorithm A' has a running time of $T'(n) = aT'\left(\frac{n}{4}\right) + n^2$. What is the largest integer value for a such that A' is asymptotically faster than A?
- 10. (15%) Consider the following undirected graph G=(V,E).

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考試科目 (代碼):2301

共_4_頁,第_4_頁 *請在【答案卷、卡】作答



- (A) (5%) Draw the process of finding a minimum spanning tree using Kruskal's algorithm.
- (B) (5%) Draw the process of solving the single-source shortest path problem with node n1 as the source vertex using Dijkstra's algorithm.
- (C) (5%) Starting from n1, find the Depth-First Search (DFS) traversal sequence of G (the priority of node is inversely proportional to the weight of incident edge).
- 11. (18%) Given an ordered file with keys 1, 2, ..., 16, determine the number of key comparisons made by a search algorithm A while searching for a specific key K.
 - (A) (3%) A is the binary search algorithm and K is 2.
 - (B) (3%) A is the binary search algorithm and K is 10.
 - (C) (3%) A is the binary search algorithm and K is 15.
 - (D) (3%) A is the Fibonacci search algorithm and K is 2.
 - (E) (3%) A is the Fibonacci search algorithm and K is 10.
 - (F) (3%) A is the Fibonacci search algorithm and K is 15.
- 12. (7%) Given a store of *n* items, what's is the least upper bound (in Big-O notation) of the running time of the solutions to the following problems:
 - (A) (3%) Fractional knapsack problem;
 - (B) (4%) General 0/1 knapsack problem.