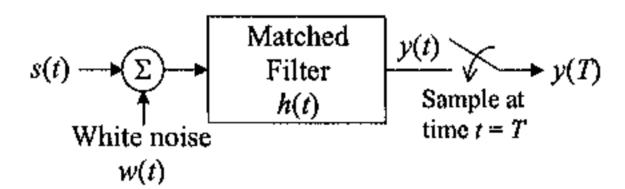
國 立 清 華 大 學 命 題 紙

九十二學年度 <u>通訊工程/電機工程研究所</u> <u>甲/乙</u> 組碩士班研究生招生考試 科目 <u>通訊系統</u> 科號 <u>3002/2404</u> 共 <u>3</u> 頁第 <u>1</u> 頁 *請在試卷【答案卷】內作答

- 1. A message signal with bandwidth equal to 4.7 kHz and amplitude in the range of (-10, 10) volts is transmitted via a PCM system. The maximum acceptable quantization error is less than 0.5 volt and the sampling rate is $R_s \times 10^3$ samples/sec, where R_s is an integer.
 - (a) What is the minimum required bandwidth (in bps) for the transmission? (5%)
 - (b) If the quantization error is modeled as a thermal noise, and the transmission bandwidth is extended to 80 kbps, what is the gain of output SNR as compared to (a)? (5%)

[Note: You must give detail derivations, otherwise you get no points.]

2. A pulse signal s(t), $0 \le t \le T$, with Fourier transform pair S(t) is received by a matched filter h(t), and the output waveform is y(t). The output signal y(T) is obtained by sampling y(t) at t = T.



- (a) Determine the frequency response of this matched filter H(f). (5 %)
- (b) Find the output signal y(T). (5 %)
- (c) If the two-sided power spectral density of w(t) is $N_0/2$, find the output SNR. (5 %)

[Note: Express the answers in terms of S(f). You must give detail derivations, otherwise you get no points.]

- 3. A white Gaussian noise w(t) with zero mean and two-sided power spectral density $N_0/2$ is filtered by an ideal band-pass filter with passband magnitude response equal to one, midband frequency f_c , and bandwidth 2B. The filtered noise is denoted as n(t).
 - (a) According to the power spectral density of n(t), find the autocorrelation function of n(t). (5 %)
 - (b) The representation of n(t) in terms of its in-phase and quadrature components is $n(t) = n_I(t)\cos(2\pi f_c t) n_Q(t)\sin(2\pi f_c t)$. According to the result of (a), find the autocorrelation functions of $n_I(t)$ and $n_Q(t)$. (5%)
 - (c) According to the result of (b), find the power spectral density of $n_I(t)$ and $n_Q(t)$. (5 %)

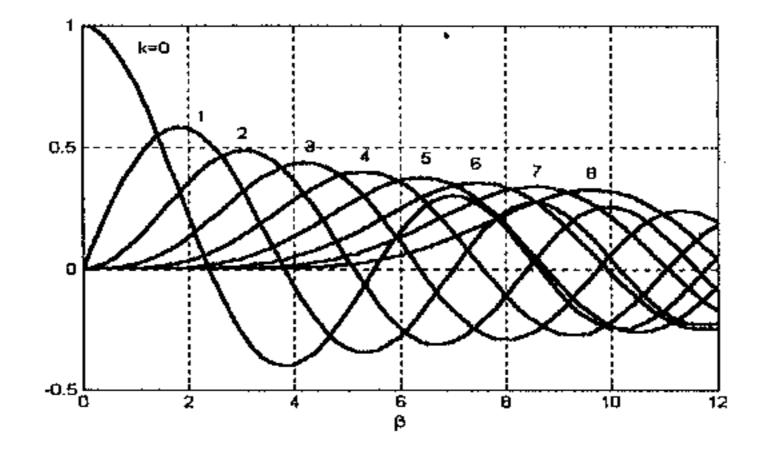
[Hint:
$$\operatorname{sinc}(2Wt) \xleftarrow{\text{Fourier Transform}} \rightarrow \frac{1}{2W} \operatorname{rect}\left(\frac{f}{2W}\right)$$
]

[Note: You must give detail derivations, otherwise you get no points.]

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- 4. A signal's power is defined as $P_s = \lim_{T \to \infty} \left\{ \frac{1}{2T} \int_{-T}^{T} |s(t)|^2 dt \right\}$.
 - (a) Assume an amplitude modulation signal: $s(t) = A_c(a_0 + m(t)) \cdot \cos(2\pi f_c t)$, where $m(t) = A_m \cos(2\pi f_m t)$ is the baseband signal with amplitude A_m and frequency f_m , and A_c and f_c are the carrier's amplitude and frequency, respectively. If no overmodulation for all t, what is the power, P_s , carried by this AM signal? (7%)
 - (b) If a carrier with an amplitude, A_c , of 2 Volts is modulated with a sine wave m(t) having a frequency at 10 kHz and a power of 2 Watts, assumed across 1- Ω resistor. The modulated signal is to have a power, P_s , of 10 Watts. What is the power in the carrier component? (3 %)
 - (c) Same as (a), but the signal is now in frequency modulation format, the signal can be written as $s(t) = A_c \cos(2\pi f_c t + 2\pi \Delta_f \left[m(t) dt \right) = A_c \sum_{-\infty}^{\infty} J_n(\beta) \cos \left[2\pi (f_c + n f_m) t \right], \text{ where } \Delta_f \text{ is the frequency}$ deviation and β is a function of Δ_f . Express β in terms of A_m , f_m , Δ_f and what is the power, P_s , carried by this FM signal? The definition of the kind function Bessel first İS $J_n(\beta) = (1/2\pi) \int_{-\pi}^{\pi} \exp[j(\beta \sin(x) - nx)] dx \quad (7\%)$
 - (d) Refer to the *n*th order Bessel function of the first kind plot shown as below, please estimate how much frequency deviation, in terms of f_m , should be if the power of the carrier component is 0? (3 %)



- 5. (a) If a filter has a unit gain and linear phase function $H(\omega) = \exp(-j\alpha\omega)$, what happens to the input signal? (5 %)
 - (b) A differentiator has the filter transform function $H(\omega) = j\omega$. If the input is a random process x(t) and output is y(t), what is the relationship between the input and output autocorrelation, $R_x(\tau)$ and $R_y(\tau)$? (5%)

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6. Consider the M-ary Coherent Frequency-Shift Keying (FSK), for which the transmitted signals are defined by

$$s_l(t) = \sqrt{\frac{2E}{T}} \cos \left[\frac{\pi}{T} (n_c + i)t \right], \quad 0 \le t \le T,$$

where i=1, 2, ..., M and the carrier frequency $f_c = n_c/2T$ for some fixed integer n_c . The transmitted symbols are of equal duration and have equal energy E with equal prior probability 1/M.

- (a) In the presence of additive white Gaussian noise with power spectral density equal to $N_0/2$, design the optimum receiver with minimum probability of symbol error. (8 %)
- (b) Find the minimum symbol error rate, P_e for M=2. For M>2, find the union bound for P_e in terms of complementary error function $\operatorname{erfc}(u)$ or in terms of Q-function Q(u) where

$$\operatorname{erfc}(u) = \frac{2}{\sqrt{\pi}} \int_{u}^{\infty} \exp(-z^{2}) dz = 2Q(\sqrt{2}u) \text{ and}$$

$$Q(u) = \frac{1}{\sqrt{2\pi}} \int_{u}^{\infty} \exp(-z^{2}/2) dz \cdot (7\%)$$

[Hint: The Gaussian distribution is $f_X(x) = \frac{1}{\sqrt{2\pi}\sigma_X} \exp\left[-\frac{(x-\mu_X)^2}{2\sigma_X^2}\right]$.]

- 7. Let s(t) denote the signal of coherent binary Phase-Shift Keying (BPSK) signal with energy per bit E_b , bit duration T_b and carrier frequency f_c .
 - (a) Express s(t) in terms of E_b , T_b and f_c . What is the associated DS/BPSK signal x(t) with the spreading factor N? (7%)
 - (b) Design a receiver to detect the data sequence from the received signal y(t) = x(t) + j(t) where j(t) is the interference signal. (8 %)