

八十五學年度 材料科學工程研究所(系(所)) 甲三 組碩士班研究生入學考試  
科目 近代物理(I) 科號 1901 共 2 頁第 1 頁 \*請在試卷【答案卷】內作答  
2001

1. Assume that there is a transparent object with refractive index  $n$ , and length  $L$ . Light can emit from one end, propagate inside of the object, and reflect back from the other end. When the object is at rest, the time for light to make a round trip is measured by an observer to be  $t$ .
  - (i) Let the object move with speed  $V$  in the direction perpendicular to the light propagation. What is the time the observer measured for light to make a round trip? (10%)
  - (ii) If the object move with the same speed, but in the direction of light propagation, what is the time the observer measured for light to make the same round trip? (10%)
2. State four experiments and explain how the results support the particle-like properties of light. (20%)
3.
  - (i) State the de Broglie's hypothesis for wave-particle relationship. (5%)
  - (ii) Use the hypothesis to show that the group velocity of a de Broglie wave  $V_g$  equals to the velocity  $V$  of the same particle. (5%)

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4. Compare the uncertainty in the momentum of an electron confined to a region of linear dimension  $a_0$  with the momentum of an electron in a ground-state Bohr orbit. (10%)
5. For single-photon excitation of the first excitation state of hydrogen, only 10.2eV photons will work. However, any single electron with K.E. > 10.2eV will work. Explain. (5%)
6. Please explain (a) induced absorption, (b) spontaneous emission, and (c) induced emission. (3%)
7. Please state principle of the three-level laser. (7%)
8. The only way for the wave function to be constant in a certain region of space is for the kinetic energy to be zero there. Prove this condition by using the one-dimensional, time independent, nonrelativistic Schrödinger wave equation. (13%)
9. The semiclassical amplitude,  $A$ , of a harmonic oscillator can be obtained from  $\frac{1}{2}m\omega_c^2 A^2 = E$ . Show that  $A$  is quantized and find its allowed values. Why can  $|x|$  be greater than  $A$ ? (12%)